

## Sec. 6.1 Vertical and Horizontal Shifts

### Transformations –

- Vertical Shifts** – Moves an entire graph up or down. When  $y = f(x)$  is transformed to  $y = f(x) + k$  or  $(-k)$ , the graph is shifted vertically up or down.

Ex. Graph  $f(x) = x^2$   
 $f(x) = x^2 - 4$  *shifted down 4*  
 $f(x) = x^2 + 6$  *shifted up 6*

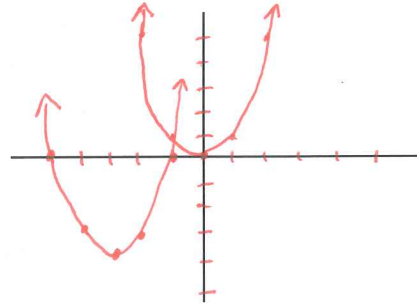
What do you notice happens to the graphs?

- Horizontal Shifts** – Moves an entire graph left or right. When  $y = f(x)$  is transformed to  $y = f(x + k)$  or  $(-k)$ . Graph moves left if it is  $+k$  and right if  $-k$ .

Ex. Graph  $f(x) = x^2$   
 $f(x) = (x - 3)^2$  *shifted 3 to right*  
 $f(x) = (x + 2)^2$  *shift 2 to left*

What do you notice happens to the graphs?

Ex. Tell what happened to  $y = (x + 3)^2 - 4$ . Then graph by hand using  $y = x^2$  as the transformation base.



Ex. Determine the equation of the graph whose vertex is  $(-3, 5)$  and whose y-intercept is  $-4$ . Then find the graph's maximum or minimum value. Also tell how the graph has moved from the original quadratic function.

$$y = a(x-h)^2 + k$$

$$y = a(x+3)^2 + 5$$

$$-4 = a(0+3)^2 + 5$$

$$-4 = 9a + 5$$

$$-9 = 9a$$

$$-1 = a$$

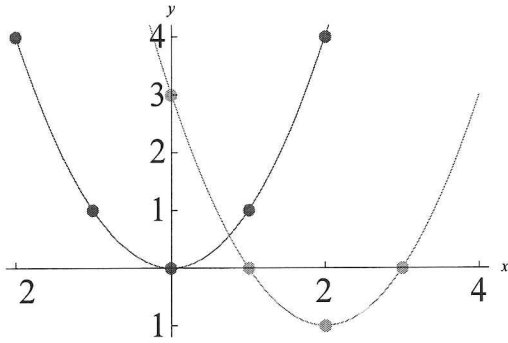
$$y = -(x+3)^2 + 5$$

*↑ opens downward*

**MAX VALUE AT**  
**VERTEX  $(-3, 5)$**

*Shifted left three and up 5.*

**Example 1** A graph of  $f(x) = x^2$  is shown in blue. Define  $g$  by shifting the graph of  $f$  to the right 2 units and down 1 unit; the graph of  $g$  is shown in red. Find a formula for  $g$  in terms of  $f$ . Find a formula for  $g$  in terms of  $x$ .



$$\boxed{g(x) = f(x-2) - 1} \leftarrow g \text{ in terms of } f$$

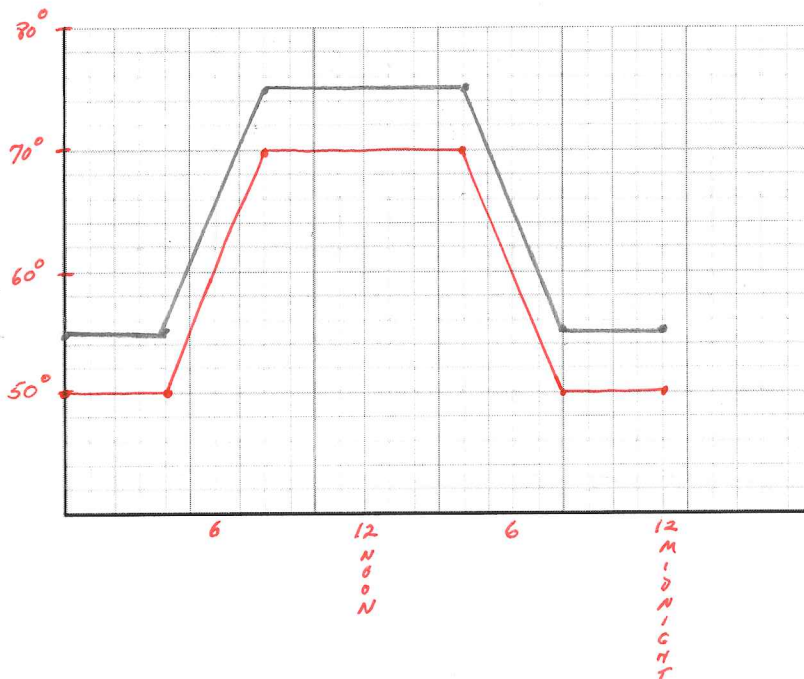
$$= (x-2)^2 - 1$$

$$= x^2 - 4x + 4 - 1$$

$$\boxed{g(x) = x^2 - 4x + 3}$$

**Example 2:** To save money, an office building is kept warm only during business hours. At midnight ( $t = 0$ ), the building's temperature ( $H$ ) is 50 F. This temperature is maintained until 4 am. Then the building begins to warm up so that by 8 am the temperature is 70 F. At 4 pm the building begins to cool. By 8 pm, the temperature is again 50 F. Suppose that the building's superintendent decides to keep the building 5 F warmer than before.

- Graph the original office temperature with temperature as a function of time.
- Graph the new office temperature with temperature as a function of time.
- Write an equation that compares the original office temperature with the new office temperature.



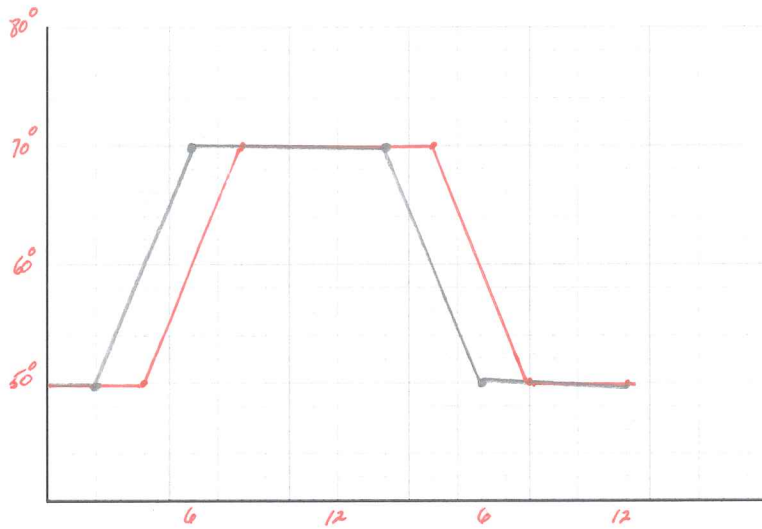
OLD TEMP:  $H(t)$

NEW TEMP:  $H(t) + 5$

$$\boxed{N(t) = H(t) + 5}$$

**Example 3:** The superintendent then changes the original heating schedule to start two hours earlier. The building now begins to warm at 2 am instead of 4 am, reaches 70 F at 6 am instead of 8 am, begins cooling off at 2 pm instead of 4 pm, and returns to 50 F at 6 pm instead of 8 pm. How are these changes reflected in the graph of the heating schedule?

- Graph the original heating schedule. See previous example for info.
- Graph the new heating schedule from Example 3.
- Write an equation that relates the original heating schedule with the new one.
- Can you write an equation that would relate the new heating schedule in Example one and Example two at the same time?



$H(t)$  = original schedule

$$N(t) = H(t+2)$$

$$N(2) = H(2+2)$$

↑

New Schedule = Old Schedule  
at 2:00 = at 4:00

HW: pg 229-233 #3-54 (m/3)

Describe transformations in 15, 18, 21, and 24 but do not graph.

Skip 42c.